

14 (1) Considering symmetry, the solutions of the equation are $\alpha, \beta, \gamma = -\alpha, \delta = -\beta$, thus.

$$\begin{aligned}x^4 + ax^3 + bx^2 + cx + d &= (x - \alpha)(x - \beta)(x + \alpha)(x + \beta) \\ &= (x^2 - \alpha^2)(x^2 - \beta^2) \\ &= x^4 - (\alpha^2 + \beta^2)x^2 + \alpha^2\beta^2 \quad \dots \textcircled{1}\end{aligned}$$

Comparing coefficients.

(2)(3) by means of $\textcircled{1}$, $b = -(\alpha^2 + \beta^2)$, $d = \alpha^2\beta^2$, then. $\dots ans.$

$$\begin{aligned}b^2 = 3d &\iff (\alpha^2 + \beta^2)^2 = 3\alpha^2\beta^2 \\ &\iff \alpha^4 - \alpha^2\beta^2 + \beta^4 = 0 \\ &\iff \left(\frac{\beta}{\alpha}\right)^4 - \left(\frac{\beta}{\alpha}\right)^2 + 1 = 0 \\ &\iff \left(\frac{\beta}{\alpha}\right)^2 = \frac{1 \pm \sqrt{3}i}{2} = \cos(\pm 60^\circ) + i \sin(\pm 60^\circ)\end{aligned}$$

Set $\beta = \alpha(\cos \theta + i \sin \theta)$ ($0 < \theta < 180^\circ$), then .

$$\begin{aligned}\cos 2\theta + i \sin 2\theta &= \cos(\pm 60^\circ) + i \sin(\pm 60^\circ) \\ \therefore \theta &= 30^\circ, 150^\circ\end{aligned}$$

Therefore, the angle formed by two diagonals of the rectangle $ABCD$ is.

$$30^\circ \quad \dots ans.$$

In addition, the length of the sides of the rectangle $ABCD$ are.

$$\frac{\sqrt{6} \pm \sqrt{2}}{2} \quad \dots ans.$$